

TABLE VII
COMPARISON ON THE PERFORMANCE OF ECHT-DE AND ECHT-ARMOR-DE FOR FUNCTIONS IN THE CEC 2010 TEST SUITE AT $D = 30$.

Prob	ECHT-DE						ECHT-ARMOR-DE					
	Best	Median	Worst	Mean	Std	F/R	Best	Median	Worst	Mean	Std	F/R
C01	-8.2170E-01	-8.0120E-01	-7.5570E-01	-7.9940E-01	1.79E-02	1.00	-8.1806E-01	-8.0029E-01	-7.3601E-01	-7.8992E-01	2.51E-02	1.00
C02	-2.2251E+00	-2.0662E+00	-1.3511E+00	-1.9943E+00	2.10E-01	1.00	-2.2607E+00	-2.1900E+00	-1.9746E+00	-2.1706E+00	7.36E-02	1.00
C03	3.2433E-21	1.0983E+02	1.8496E+02	9.8920E+01	6.26E+01	1.00	2.5801E-24	2.8673E+01	2.8673E+01	2.6380E+01	7.94E+00	1.00
C04	-3.3015E-06	-2.9456E-06	4.6205E-01	-1.0257E-06	9.01E-02	1.00	-3.3326E-06	9.9236E-05	1.0886E+00	8.3713E-02	2.89E-01	1.00
C05	-2.1368E+02	-1.6300E+02	4.7719E+02	-1.0642E+02	1.67E+02	1.00	-4.8122E+02	-4.7647E+02	7.6414E+01	-4.3335E+02	1.46E+02	1.00
C06	-2.9572E+02	-1.4732E+02	2.6353E+02	-1.3762E+02	9.89E+01	1.00	-5.3010E+02	-5.2465E+02	1.2454E+02	-4.8931E+02	1.32E+02	1.00
C07	0.0000E+00	0.0000E+00	3.9866E+00	1.3290E-01	7.28E-01	1.00	0.0000E+00	3.4286E-26	1.1045E-24	1.0789E-25	2.20E-25	1.00
C08	0.0000E+00	0.0000E+00	5.8567E+02	3.3585E+01	1.11E+02	1.00	0.0000E+00	8.5541E-26	1.5113E+02	2.0101E+01	4.70E+01	1.00
C09	0.0000E+00	0.0000E+00	6.5710E+02	4.2441E+01	1.38E+02	1.00	0.0000E+00	2.2153E-25	1.1527E+02	4.6110E+00	2.31E+01	1.00
C10	0.0000E+00	3.1309E+01	4.7510E+02	5.3381E+01	8.83E+01	1.00	6.0209E-13	3.1309E+01	5.3332E+02	6.5536E+01	1.07E+02	1.00
C11	-4.0000E-04	-2.0000E-04	2.0400E-02 [‡]	2.6000E-03	6.00E-03	NA	-3.9234E-04	-3.9234E-04	1.8671E-02 [‡]	1.1327E-03	5.28E-03	0.92
C12	-1.9930E-01	-1.9930E-01	-7.4816E+02 [‡]	-2.5129E+01	1.37E+02	NA	-1.9926E-01	-1.9926E-01	7.6343E-01	-1.6076E-01	1.93E-01	1.00
C13	-6.8429E+01	-6.4619E+01	-6.0939E+01	-6.4583E+01	1.67E+00	1.00	-6.7416E+01	-6.4908E+01	-6.0769E+01	-6.4646E+01	1.97E+00	1.00
C14	0.0000E+00	0.0000E+00	3.7101E+06	1.2368E+05	6.77E+05	1.00	1.5809E-27	4.4875E-26	1.1507E+04	6.6135E+02	2.47E+03	1.00
C15	1.9922E+09	8.5527E+10	2.3252E+12	1.9409E+11	4.35E+11	1.00	1.1716E-04	2.1603E+01	5.9937E+09	3.1316E+08	1.20E+09	1.00
C16	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.00E+00	1.00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.00E+00	1.00
C17	0.0000E+00	1.9273E-01	1.8986E+00	2.7496E-01	3.78E-01	1.00	3.3564E-16	4.2103E-01	1.2633E+00	4.0336E-01	3.51E-01	1.00
C18	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.00E+00	1.00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.00E+00	1.00

‡ indicates the solution is infeasible.

TABLE VIII
COMPARED THE RESULTS OF ECHT-ARMOR-DE WITH OTHER EAS FOR FUNCTIONS IN THE CEC 2010 TEST SUITE AT $D = 30$.

Prob	ECHT-DE	AIS-ZYH	ϵ DEg	IEMA	ECHT-ARMOR-DE
C01	-7.9940E-01 \pm 1.79E-02	-8.2011E-01 \pm 3.25E-04	-8.2087E-01 \pm 7.10E-04	-8.1777E-01 \pm 4.79E-03	-7.8992E-01 \pm 2.51E-02
C02	-1.9943E+00 \pm 2.10E-01	-2.2125E+00 \pm 2.84E-03	-2.1745E+00 \pm 1.20E-02	-1.5045E+00 \pm 2.14E+00	-2.1706E+00 \pm 7.36E-02
C03	9.8920E+01 \pm 6.26E+01	6.6758E+01 \pm 4.26E+02	2.8838E+01 \pm 8.00E-01	-	2.6380E+01 \pm 7.94E+00
C04	-1.0257E-06 \pm 9.01E-02	1.9761E-03 \pm 1.61E-03	8.1630E-03 \pm 3.06E-03	-	8.3713E-02 \pm 2.89E-01
C05	-1.0642E+02 \pm 1.67E+02	-4.3611E+02 \pm 2.51E+01	-4.4955E+02 \pm 2.89E+00	-2.7093E+02 \pm 1.41E+00	-4.3335E+02 \pm 1.46E+02
C06	-1.3762E+02 \pm 9.89E+01	-4.5426E+02 \pm 4.79E+01	-5.2791E+02 \pm 4.74E-01	-1.3288E+02 \pm 5.61E+02	-4.8931E+02 \pm 1.32E+02
C07	1.3290E-01 \pm 7.28E-01	1.0730E+00 \pm 1.61E+00	2.6036E-15 \pm 1.23E-15	8.4861E-10 \pm 4.84E-10	1.0789E-25 \pm 2.20E-25
C08	3.3585E+01 \pm 1.11E+02	1.6531E+00 \pm 6.41E-01	7.8315E-14 \pm 4.85E-14	1.7703E+01 \pm 4.08E+01	2.0101E+01 \pm 4.70E+01
C09	4.2441E+01 \pm 1.38E+02	1.5654E+00 \pm 1.96E+00	1.0721E+01 \pm 2.82E+01	2.9879E+07 \pm 4.50E+07	4.6110E+00 \pm 2.31E+01
C10	5.3381E+01 \pm 8.83E+01	1.7847E+01 \pm 1.88E+01	3.3262E+01 \pm 4.54E-01	1.5834E+07 \pm 1.68E+07	6.5536E+01 \pm 1.07E+02
C11	2.6000E-03 \pm 6.00E-03 [‡]	-1.5790E-04 \pm 4.67E-05	-2.8638E-04 \pm 2.71E-05	-	1.1327E-03 \pm 5.28E-03
C12	-2.5129E+01 \pm 1.37E+02 [‡]	4.2881E-06 \pm 4.52E-04	3.5623E+02 \pm 2.89E+02 [‡]	-	-1.6076E-01 \pm 1.93E-01 [‡]
C13	-6.4583E+01 \pm 1.67E+00	-6.6236E+01 \pm 2.27E-01	-6.5353E+01 \pm 5.73E+01	-6.7487E+01 \pm 9.83E-01	-6.4646E+01 \pm 1.97E+00
C14	1.2368E+05 \pm 6.77E+05	8.6828E-07 \pm 3.14E-07	3.0894E-13 \pm 5.61E-13	6.1524E-02 \pm 3.07E-01	6.6135E+02 \pm 2.47E+03
C15	1.9409E+11 \pm 4.35E+11	3.4128E+01 \pm 3.82E+01	2.1603E+01 \pm 1.10E-04	2.2949E+08 \pm 4.64E+08	3.1316E+08 \pm 1.20E+09
C16	0.0000E+00 \pm 0.00E+00	8.2062E-02 \pm 1.12E-01	2.1684E-21 \pm 1.06E-20	1.6329E-03 \pm 8.16E-03	0.0000E+00 \pm 0.00E+00
C17	2.7496E-01 \pm 3.78E-01	3.6051E+00 \pm 2.54E+00	6.3265E+00 \pm 4.99E+00	8.8397E-02 \pm 1.51E-01	4.0336E-01 \pm 3.51E-01
C18	0.0000E+00 \pm 0.00E+00	4.0152E+01 \pm 1.80E+01	8.7546E+01 \pm 1.66E+02	4.7384E-14 \pm 6.57E-14	0.0000E+00 \pm 0.00E+00

‡ indicates that there are infeasible solutions in this function over 25 independent runs.

TABLE IX
RANKS COMPUTED BY THE WILCOXON TEST FOR STATE-OF-THE-ART EAS ON CEC 2010 BENCHMARK FUNCTIONS AT $D = 30$.

	(1)	(2)	(3)	(4)
ECHT-DE (1)	-	27.0 \circ	22.0 \circ	24.5 \circ
AIS-ZYH (2)	109.0 \bullet	-	60.0	82.0
ϵ DEg (3)	114.0 \bullet	76.0	-	95.0
ECHT-ARMOR-DE (4)	111.5 \bullet	54.0	41.0	-

TABLE XII
INFLUENCE OF DIFFERENT MODELS IN ARMOR. THE NFES_e VALUES OF ECHT-DE, ECHT-ARMOR-DE3, AND ECHT-ARMOR-DE4 FOR THE CEC 2006 FUNCTIONS ARE REPORTED.

Prob	ECHT-DE (1)			ECHT-ARMOR-DE3 (2)			ECHT-ARMOR-DE4 (3)			AR (1) vs (2)	AR (1) vs (3)
	Mean	Std	SR	Mean	Std	SR	Mean	Std	SR		
g01	1.384E+05	4.06E+03	1.00	1.011E+05	3.91E+03	1.00	1.130E+05	3.50E+03	1.00	1.37	1.22
g02	8.205E+04	6.25E+03	0.42	6.509E+04	8.91E+03	0.26	7.411E+04	2.34E+04	0.30	0.78	0.79
g03	1.161E+05	1.53E+03	1.00	1.137E+05	2.53E+03	1.00	1.150E+05	2.46E+03	1.00	1.02	1.01
g04	6.470E+04	2.43E+03	1.00	4.450E+04	1.32E+03	1.00	4.946E+04	1.44E+03	1.00	1.45	1.31
g05	1.204E+05	1.45E+03	1.00	1.196E+05	6.85E+02	1.00	1.204E+05	1.27E+03	1.00	1.01	1.00
g06	2.224E+04	1.24E+03	1.00	1.549E+04	7.53E+02	1.00	1.722E+04	7.64E+02	1.00	1.44	1.29
g07	1.088E+05	4.87E+03	1.00	7.144E+04	3.18E+03	1.00	7.645E+04	3.42E+03	1.00	1.52	1.42
g08	2.644E+03	4.15E+02	1.00	2.172E+03	2.80E+02	1.00	2.328E+03	4.17E+02	1.00	1.22	1.14
g09	4.194E+04	1.81E+03	1.00	2.956E+04	1.09E+03	1.00	3.268E+04	1.48E+03	1.00	1.42	1.28
g10	1.855E+05	7.49E+03	1.00	1.109E+05	4.18E+03	1.00	1.203E+05	5.02E+03	1.00	1.67	1.54
g11	5.820E+04	1.85E+04	1.00	6.264E+04	1.11E+04	1.00	6.178E+04	1.34E+04	1.00	0.93	0.94
g12	3.072E+03	7.83E+02	1.00	2.588E+03	5.63E+02	1.00	2.316E+03	5.38E+02	1.00	1.19	1.33
g13	1.109E+05	4.39E+03	1.00	1.090E+05	4.76E+03	1.00	1.090E+05	4.76E+03	1.00	1.02	1.02
g14	1.401E+05	6.59E+03	1.00	1.293E+05	3.06E+03	1.00	1.317E+05	3.48E+03	1.00	1.08	1.06
g15	1.083E+05	5.58E+03	1.00	1.057E+05	7.51E+03	1.00	1.074E+05	7.56E+03	1.00	1.03	1.01
g16	3.019E+04	1.37E+03	1.00	2.055E+04	9.11E+02	1.00	2.329E+04	1.19E+03	1.00	1.47	1.30
g17	1.174E+05	1.59E+03	1.00	1.168E+05	9.70E+02	1.00	1.171E+05	1.06E+03	1.00	1.00	1.00
g18	1.431E+05	2.02E+04	1.00	9.254E+04	1.26E+04	1.00	8.807E+04	1.05E+04	1.00	1.55	1.63
g19	NA	NA	0.00	1.863E+05	1.34E+04	1.00	2.016E+05	1.41E+04	1.00	NA	NA
g21	1.734E+05	6.82E+03	1.00	1.468E+05	2.57E+03	1.00	1.564E+05	3.05E+03	1.00	1.18	1.11
g23	2.274E+05	5.72E+03	0.72	1.719E+05	6.00E+03	1.00	1.799E+05	5.70E+03	1.00	1.84	1.76
g24	8.120E+03	7.81E+02	1.00	6.132E+03	3.78E+02	1.00	6.556E+03	6.01E+02	1.00	1.32	1.24
avg	-	-	0.915	-	-	0.966	-	-	0.968	1.26	1.21

TABLE XIII
COMPARISON ON THE NFES_f VALUES OF ECHT-DE, ECHT-ARMOR-DE1, AND ECHT-ARMOR-DE3 FOR THE CEC 2006 FUNCTIONS.

Prob	ECHT-DE (1)			ECHT-ARMOR-DE1 (2)			AR' (1) vs (2)	ECHT-ARMOR-DE3 (3)			AR' (1) vs (3)
	Mean	Std	FR	Mean	Std	FR		Mean	Std	FR	
g01	3.292E+03	6.14E+02	1.00	2.352E+03	3.99E+02	1.00	1.40	2.720E+03	4.64E+02	1.00	1.21
g03	4.296E+04	1.00E+04	1.00	4.375E+04	1.01E+04	1.00	0.98	4.426E+04	1.09E+04	1.00	0.97
g05	1.160E+05	2.33E+03	1.00	1.165E+05	2.11E+03	1.00	1.00	1.160E+05	2.79E+03	1.00	1.00
g06	1.448E+03	3.25E+02	1.00	1.104E+03	2.56E+02	1.00	1.31	1.168E+03	2.47E+02	1.00	1.24
g07	2.412E+03	5.35E+02	1.00	1.936E+03	3.91E+02	1.00	1.25	2.232E+03	4.49E+02	1.00	1.08
g08	2.440E+02	1.09E+02	1.00	2.360E+02	7.76E+01	1.00	1.03	2.400E+02	9.04E+01	1.00	1.02
g09	2.960E+02	1.35E+02	1.00	2.800E+02	1.07E+02	1.00	1.06	2.920E+02	1.29E+02	1.00	1.01
g10	2.480E+03	5.92E+02	1.00	1.920E+03	3.59E+02	1.00	1.29	2.040E+03	3.81E+02	1.00	1.22
g11	2.248E+04	1.35E+04	1.00	2.090E+04	1.15E+04	1.00	1.08	2.082E+04	1.14E+04	1.00	1.08
g13	1.109E+05	4.39E+03	1.00	1.092E+05	4.70E+03	1.00	1.01	1.090E+05	4.76E+03	1.00	1.02
g14	1.109E+05	6.80E+03	1.00	1.136E+05	4.79E+03	1.00	0.98	1.122E+05	6.07E+03	1.00	0.99
g15	1.033E+05	6.46E+03	1.00	1.010E+05	6.33E+03	1.00	1.02	9.962E+04	7.84E+03	1.00	1.04
g16	1.236E+03	4.38E+02	1.00	1.028E+03	3.18E+02	1.00	1.20	1.088E+03	3.86E+02	1.00	1.14
g17	1.116E+05	3.05E+03	1.00	1.129E+05	2.44E+03	1.00	0.99	1.132E+05	2.45E+03	1.00	0.99
g18	7.568E+03	6.94E+02	1.00	5.416E+03	5.83E+02	1.00	1.40	6.232E+03	7.68E+02	1.00	1.21
g21	1.095E+05	5.52E+03	1.00	1.131E+05	3.01E+03	1.00	0.97	1.127E+05	4.15E+03	1.00	0.97
g22	NA	NA	0.00	2.183E+05	1.12E+04	0.88	NA	2.273E+05	9.15E+03	0.30	NA
g23	1.061E+05	2.69E+03	1.00	1.076E+05	4.25E+03	1.00	0.99	1.060E+05	3.38E+03	1.00	1.00
avg	-	-	0.944	-	-	0.993	1.11	-	-	0.961	1.07

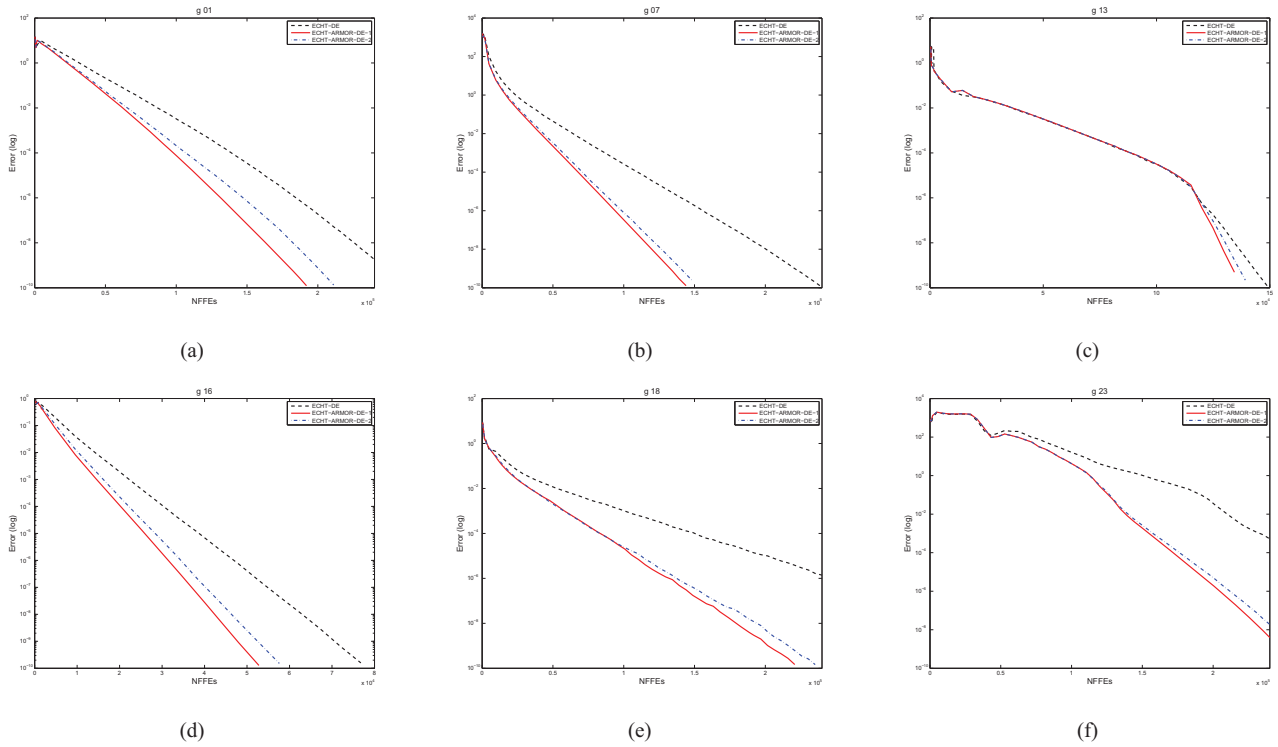


Fig. 2. Convergence graphs of ECHT-DE, ECHT-ARMOR-DE1, and ECHT-ARMOR-DE2 for the selected functions in CEC 2006. (a) g01; (b) g07; (c) g13; (d) g16; (e) g18 (f) g23.

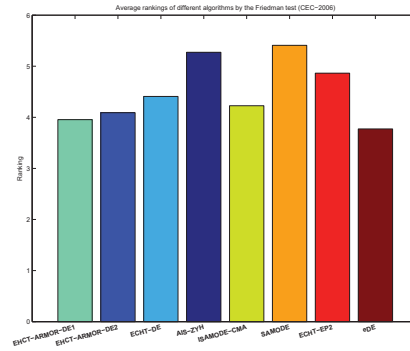


Fig. 3. Average rankings of different algorithms by the Friedman test for the CEC 2006 functions. The lower the ranking, the better the performance obtained by the algorithm. The p -value computed by the Friedman test is 0.209197.

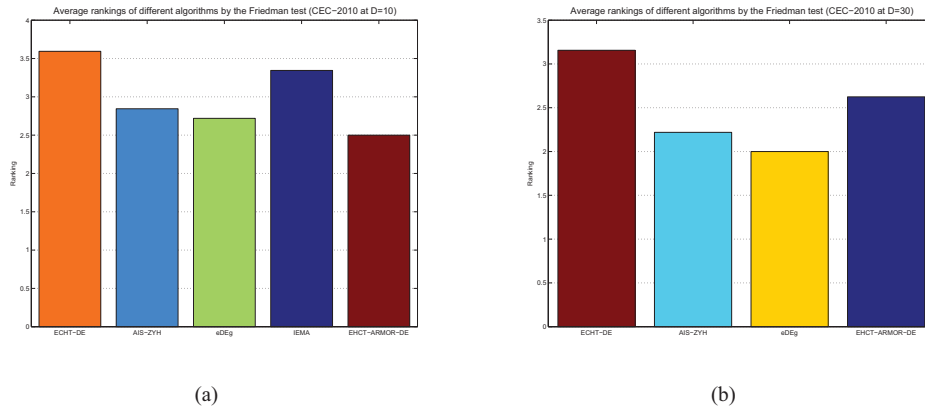


Fig. 4. Average rankings of different algorithms by the Friedman test for the CEC 2010 functions with respect to the mean quality of final solutions. (a) $D = 10$; The p -value computed by the Friedman test is 0.260226. (b) $D = 30$; The p -value computed by the Friedman test is 0.059022.